St. Vincent de Paul Catholic Primary School

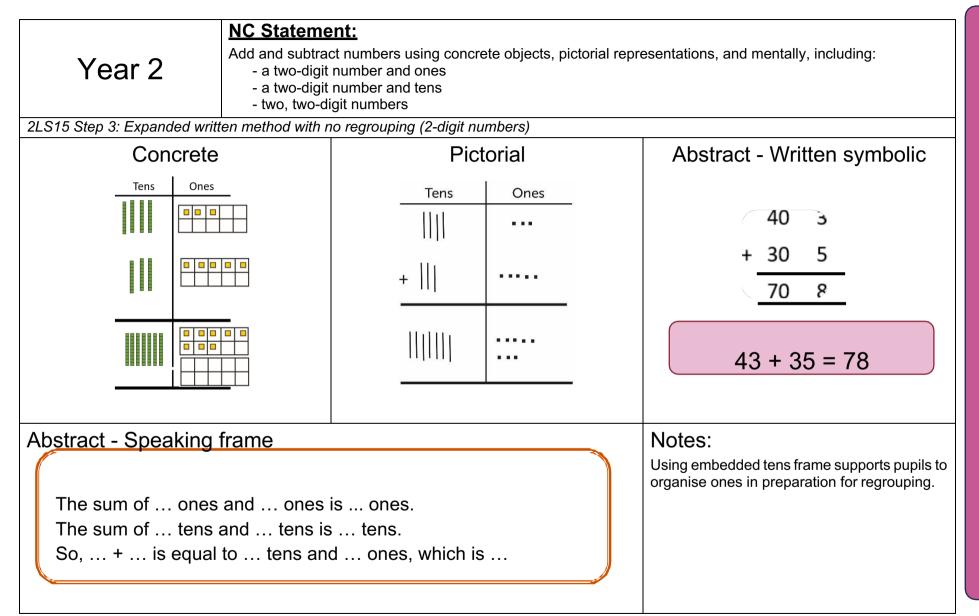


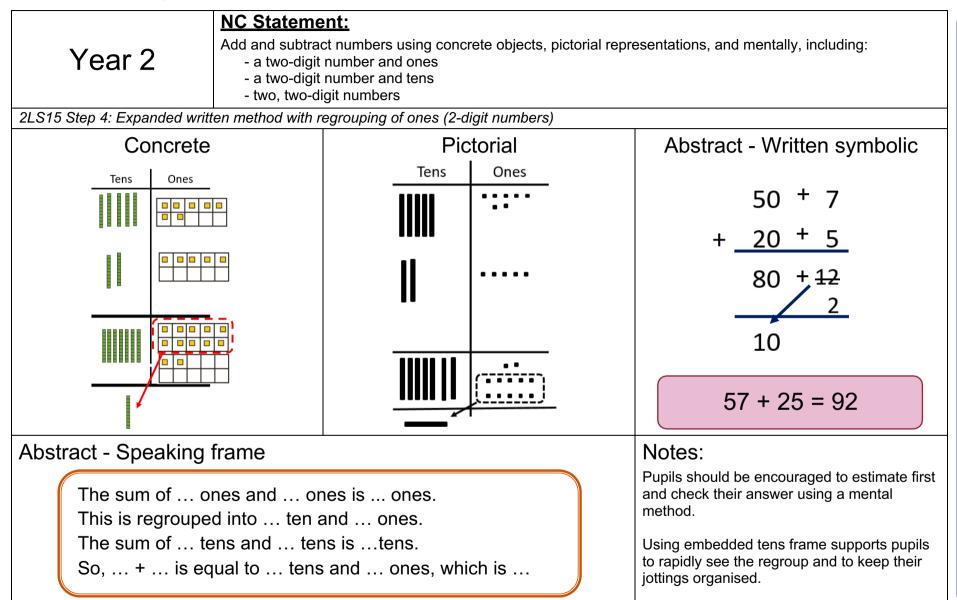
Progression in Calculation Methods KS1 & 2

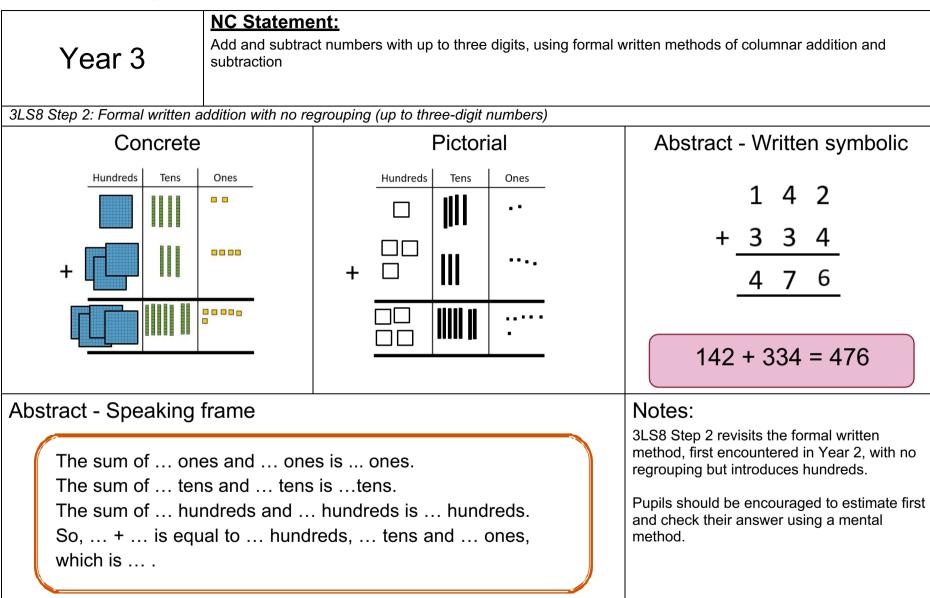
Taken from Herts For Learning (HfL)

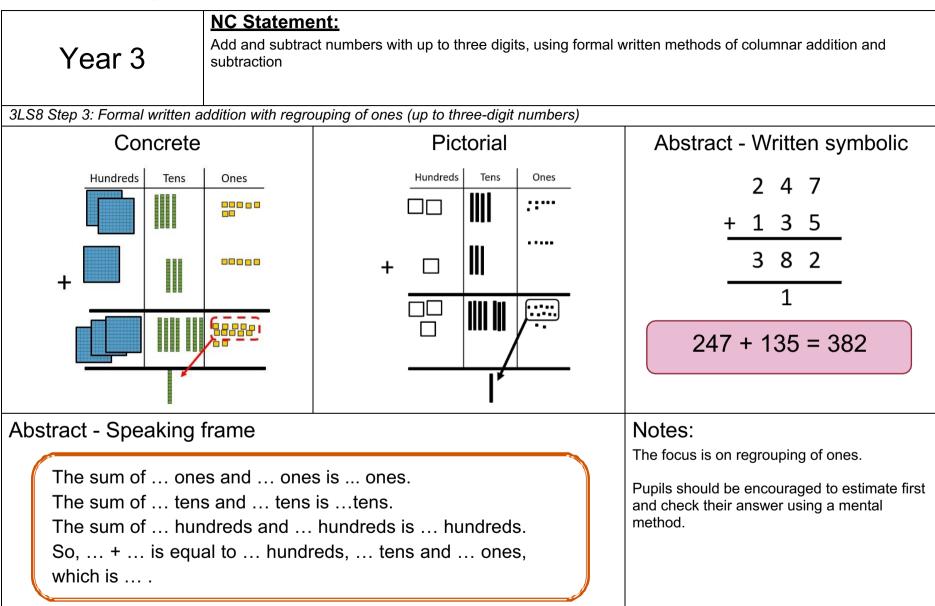
"We are called to be the hands and face of Jesus as we learn, love and grow together"

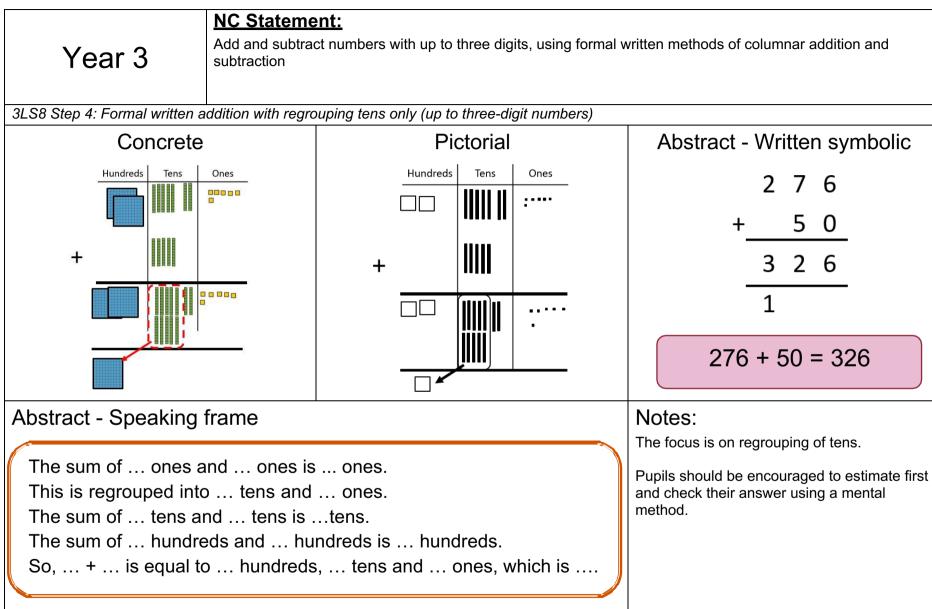
> Reviewed: Autumn 2019 To be reviewed: Spring 2022 Reviewed by the Teaching and Learning committee Subject Leaders – Mrs McGuire & Mrs Blythe



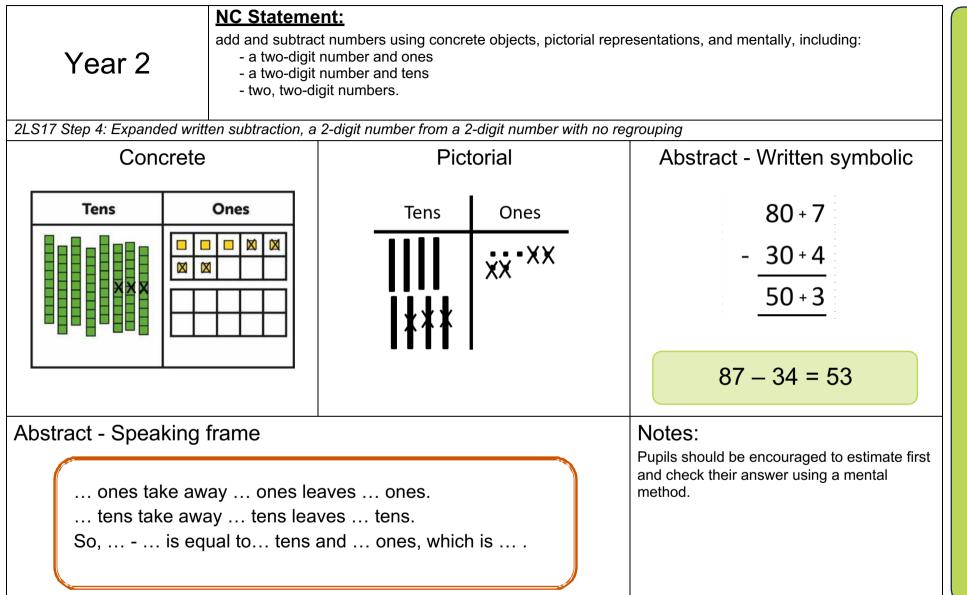


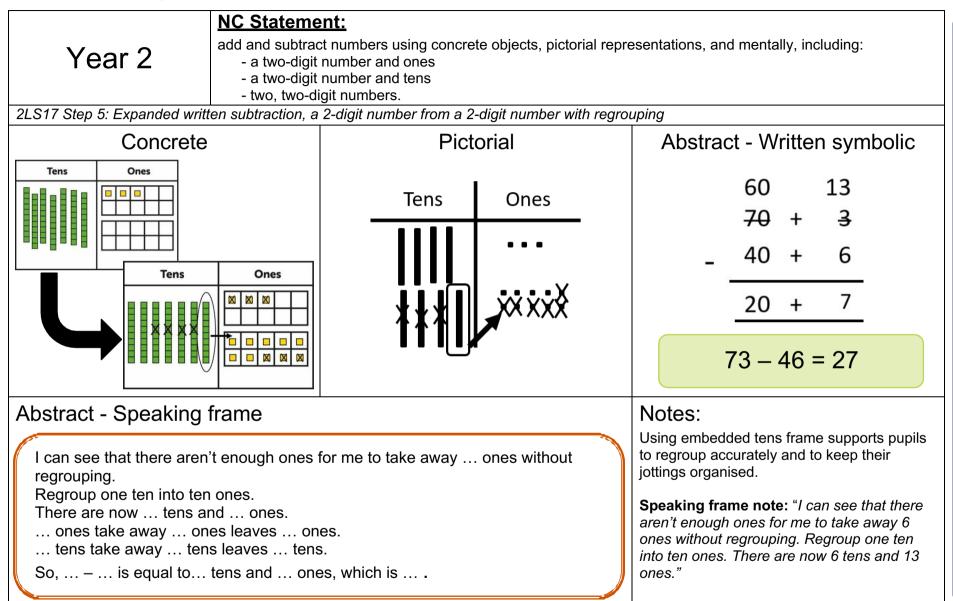


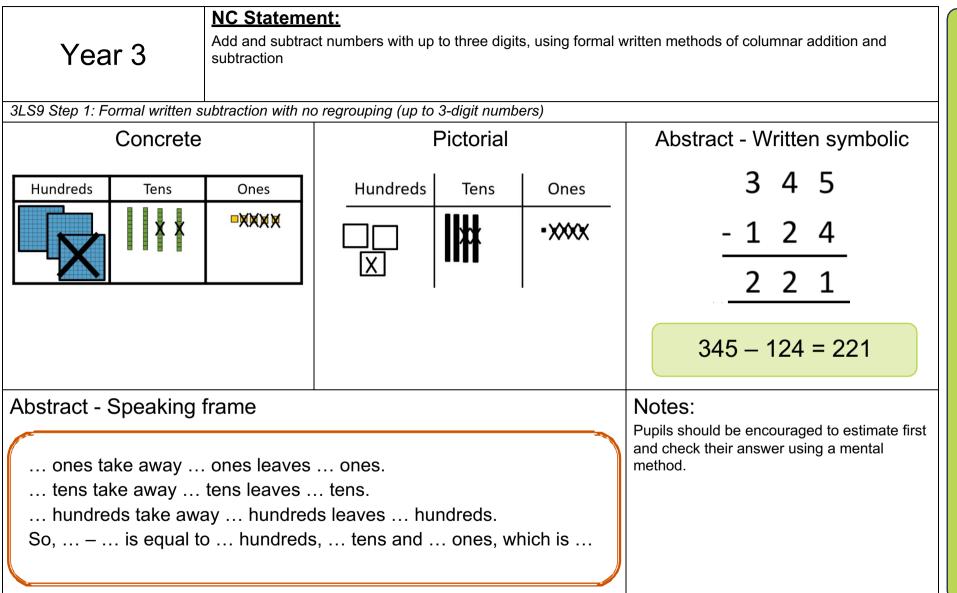


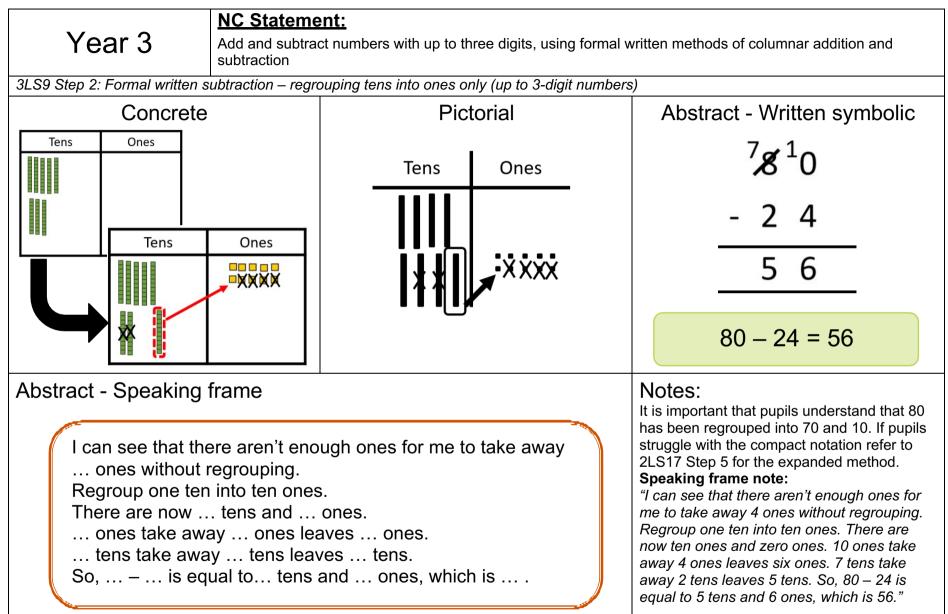


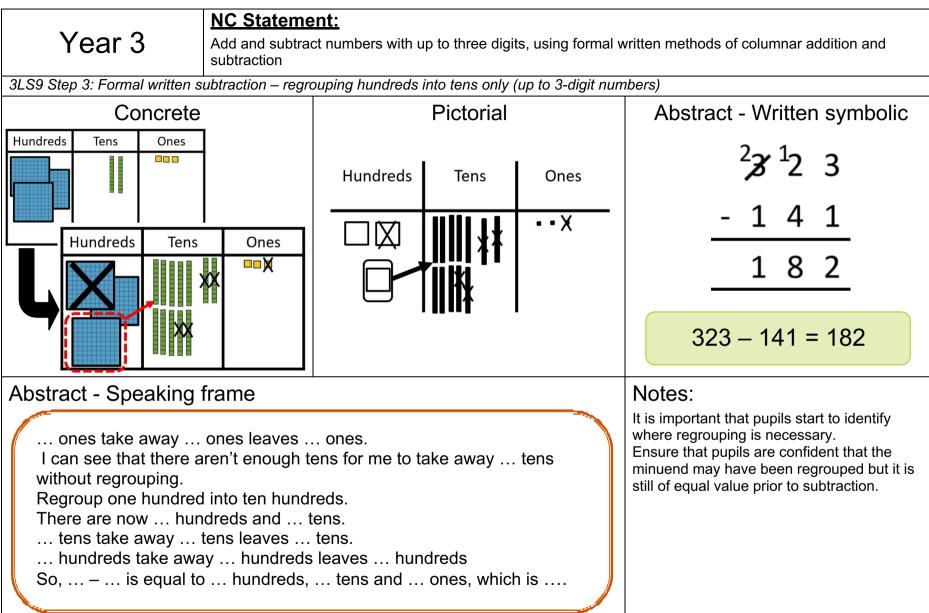
NC Statement: Year 3 Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction 3LS8 Step 4: Formal written addition with regrouping tens and ones (up to three-digit numbers) Concrete Pictorial Abstract - Written symbolic Hundreds Tens Ones Hundreds Tens Ones 5 6 + 3 2 3 + 1 1 \Box [..... 276 + 56 = 332Abstract - Speaking frame Notes: Pupils should be encouraged to estimate first and check their answer using a mental The sum of ... ones and ... ones is ... ones. method. This is regrouped into ... tens and ... ones. Once pupils have fully understood and The sum of ... tens and ... tens is ... tens. rehearsed regrouping within formal column addition of 3-digit numbers, this This is regrouped into ... hundreds and ... tens. learning continues to be rehearsed and The sum of ... hundreds and ... hundreds is ... hundreds. applied throughout Years 4, 5 and 6, So, ... + ... is equal to ... hundreds, ... tens and ... ones, which is ... including to 4-digit numbers, larger numbers, decimal numbers, money and measures.

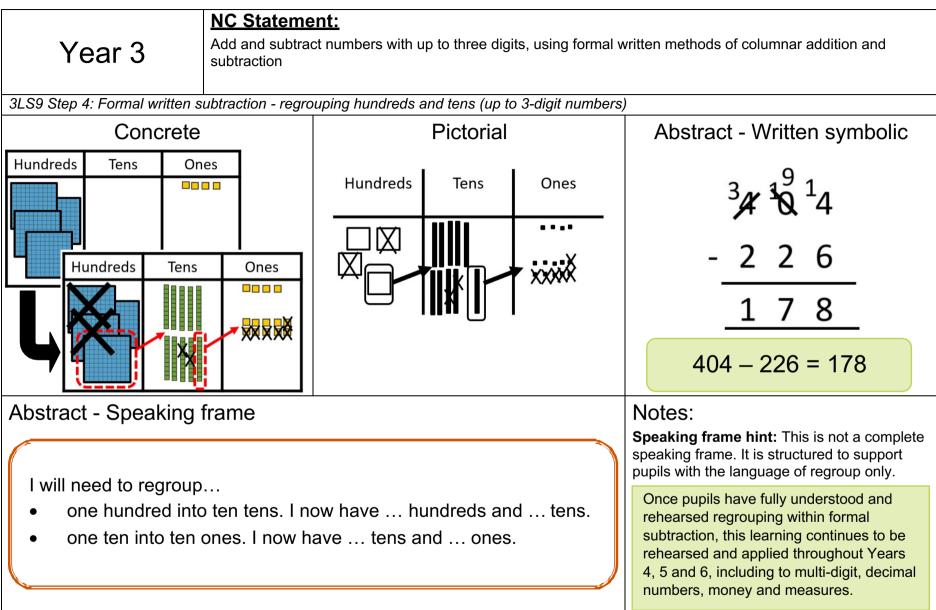






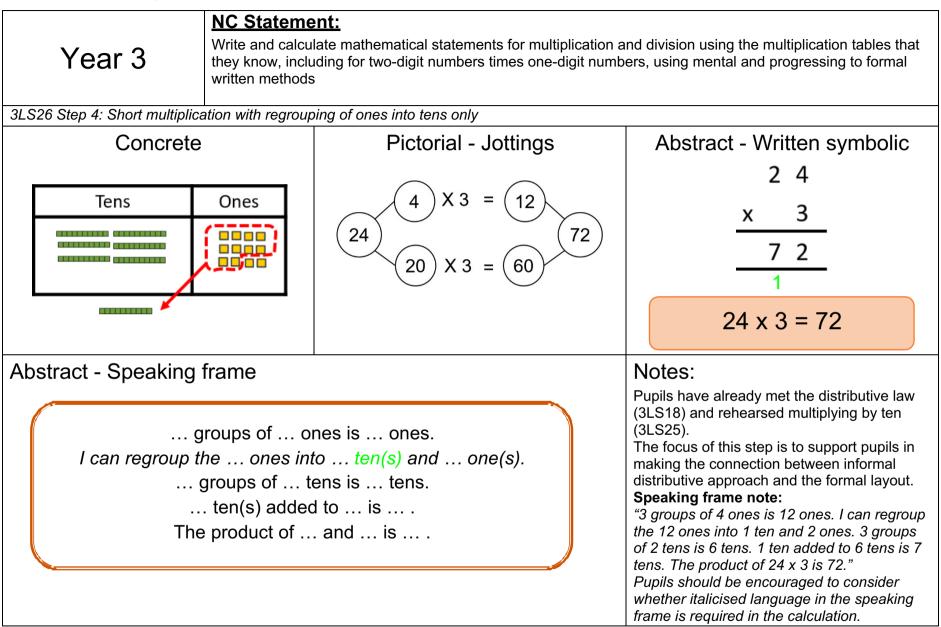


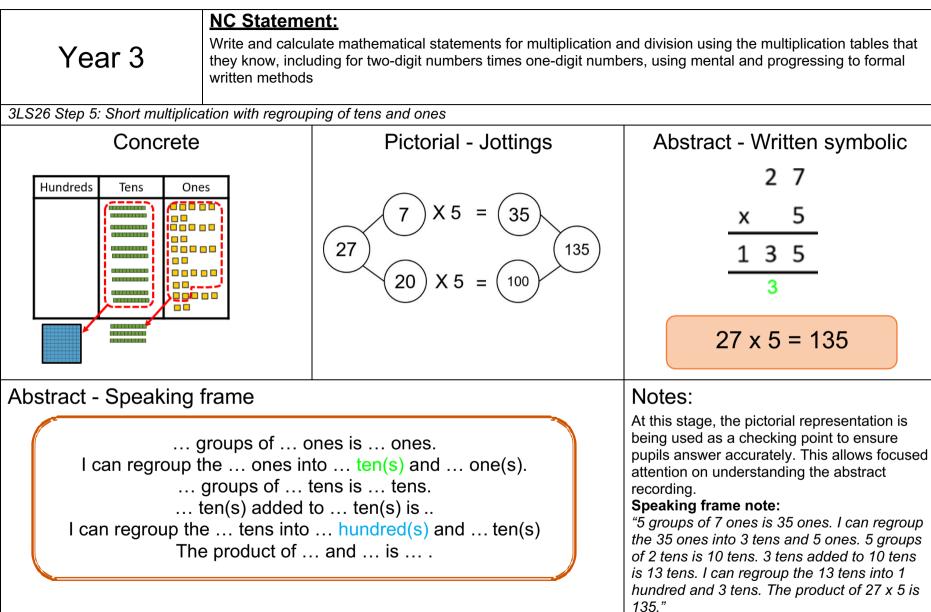


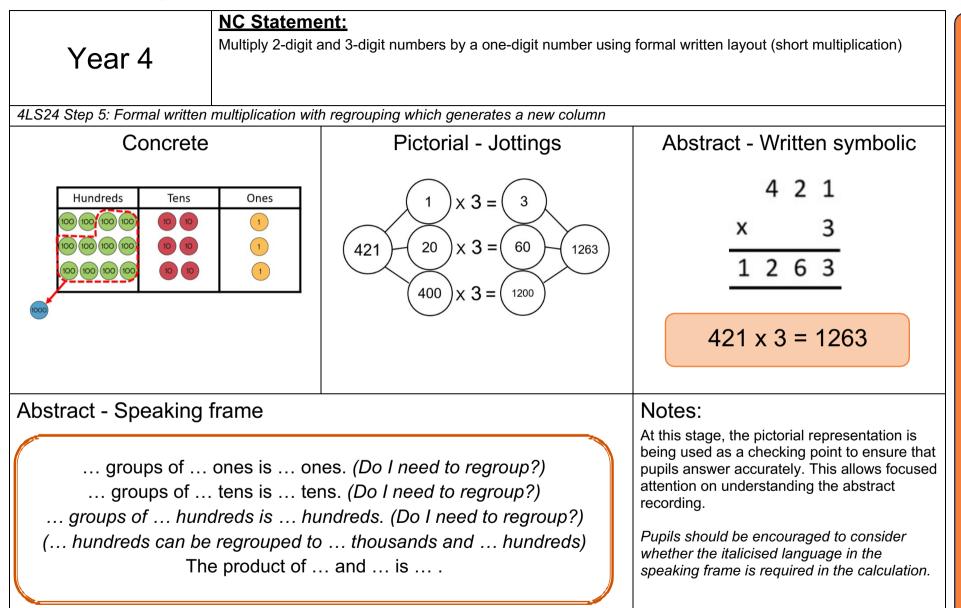


Year 3	and division using the multiplication tables that bers, using mental and progressing to formal		
3LS26 Step 3: Introducing	short multiplication w	vith no regrouping	1
Concre	ete	Pictorial - Jottings Abstract - Written sym	
	Ones	$\begin{array}{c} 2 \\ 12 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ $	$ \begin{array}{r} 1 & 2 \\ $
Abstract - Speakin	ng frame		Notes:
	groups of of of of of of of of of tens added to The product of .	tens is … tens. o … ones is	Pupils have already met the distributive law (3LS18) and rehearsed multiplying by ten (3LS25). The focus of this step is support pupils in making the connection between informal distributive approach and the formal layout. Speaking frame note: "3 groups of 2 ones is 6 ones. 3 groups of 1 ten is 3 tens. 3 tens added 6 ones is 36. The product of 12 and 3 is 36."

Multiplication







NC Statement:

Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers

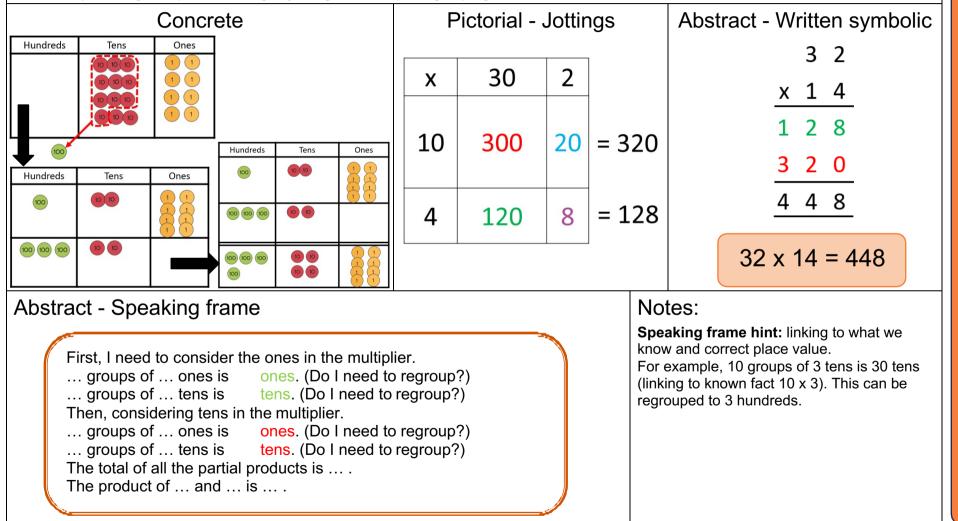
5LS11 Step 2: Expanded vertical multiplication 2-digit by 2-digit

	Concrete			Pictorial - Jottings			ngs	A	Abstract - Written symbolic		
x	30	2					20	2]		32 x14
			x	30	2	X	30	2			$\frac{x + 4}{8}$
10			10		0 0	10	300	20	= 320		1 2 0 2 0
4			4	000		4	120	8	= 128		$\frac{3 \ 0 \ 0}{4 \ 4 \ 8}$
Abs	600 00 1 1 1 1 1 1 1 1 1 1										
F T T	Abstract - Speaking frame First, I need to consider the ones in the multiplier. groups of ones is ones. groups of tens is tens. (Do I need to regro Then, tens in the multiplier. groups of ones is ones. (Do I need to regro groups of tens is tens. (Do I need to regro The total of all the partial products is The product of and is						regroup?) regroup?)			This mult in the of te of bo move succe Spe know 10 g	is a transitional method towards long iplication. Using the grid supports pupils eir thinking about multiplying by powers n and place value. Secure understanding oth of these concepts allow pupils to e to long multiplication more ressfully. aking frame hint: linking to what we v and correct place value. For example, roups of 3 tens is 30 tens. This can be puped to 3 hundreds.

NC Statement:

Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers

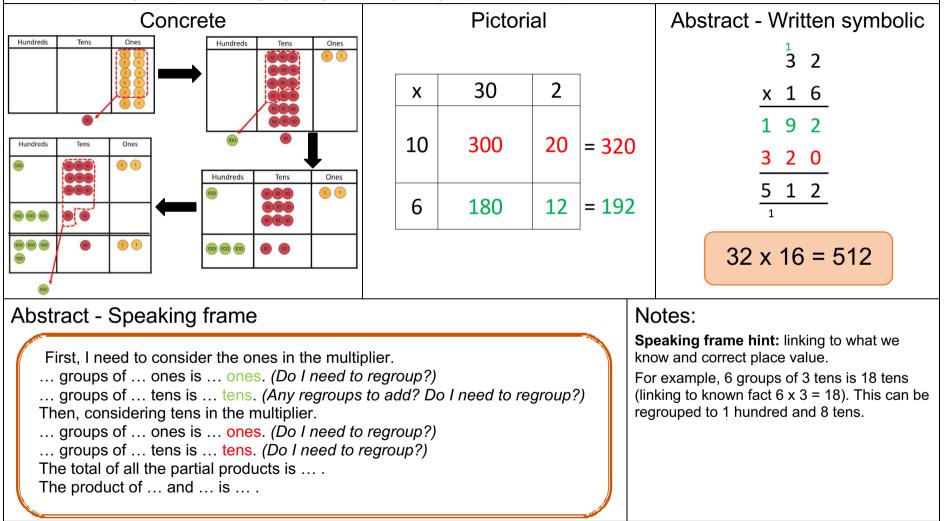
5LS11 Step 3: Long multiplication 2-digit by 2-digit with simple regrouping

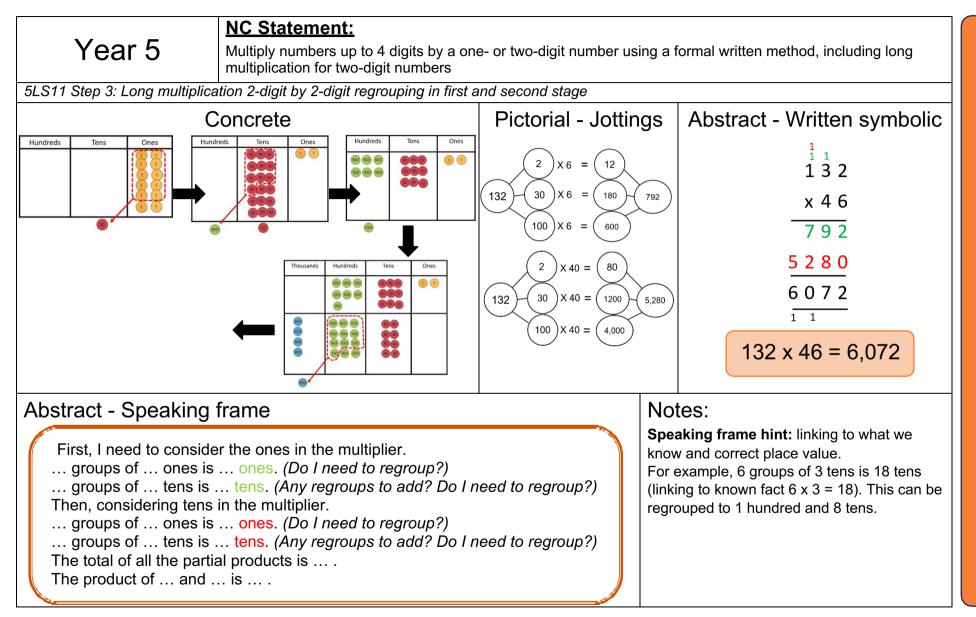


NC Statement:

Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers

5LS11 Step 3: Long multiplication 2-digit by 2-digit, focusing on regroup in first partial product





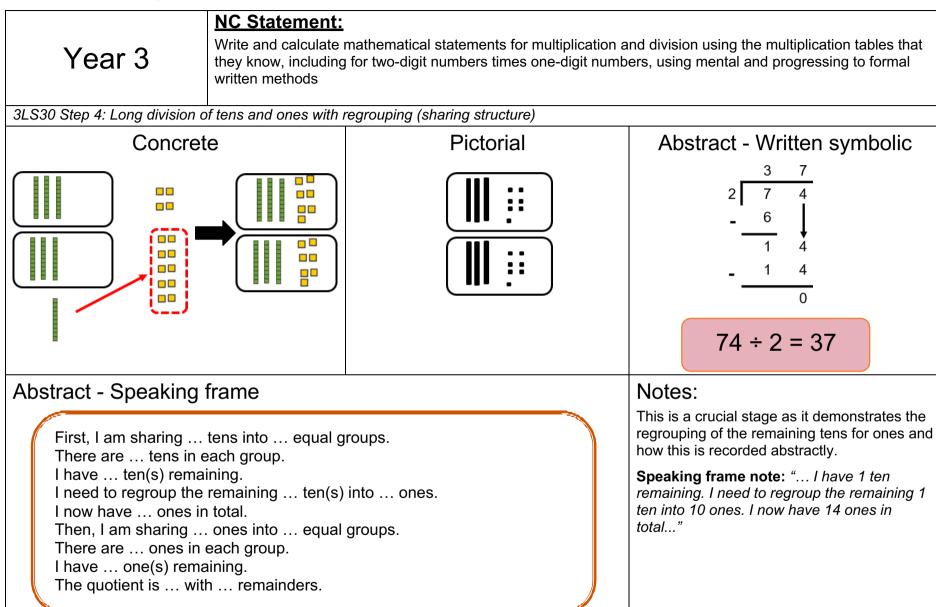
Multiplication

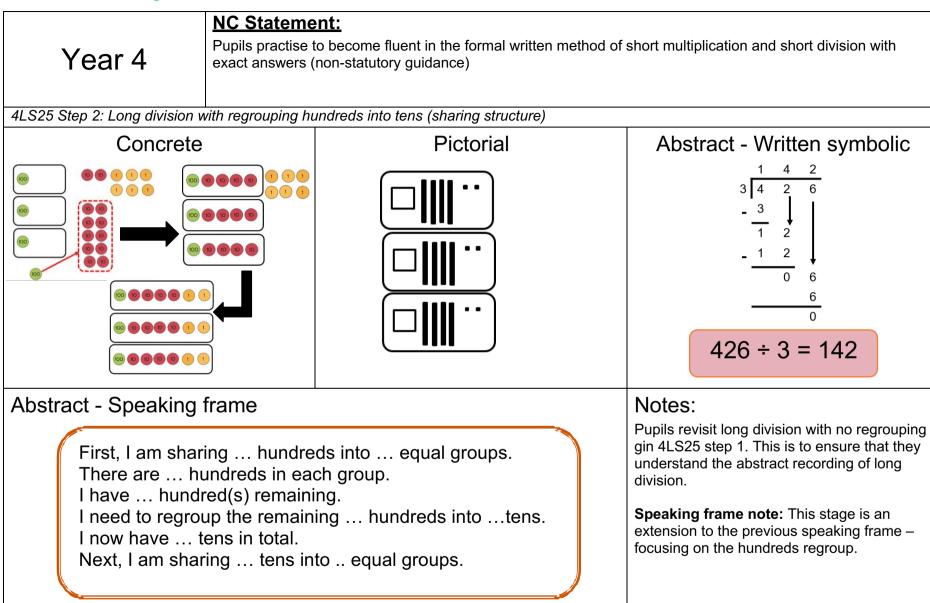
NC Statement: Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long Year 6 multiplication for two-digit numbers 6LS12 Step 5: Formal written multiplication involving numbers with up to 2 decimal places multiplied by a 1-digit number Pictorial - Jottings Abstract - Written symbolic Concrete Jottings: multiples of tricky Hundreds Tens Ones tenths Hundreds Tens tenths Ones multipliers 2 1 01 01 34.2 6 12 х 6 18 24 10 10 205.2 30 Hundreds Tens Ones tenths 36 42 01 01 48 54 $34.2 \times 6 = 205.2$ 60 66 72 Abstract - Speaking frame Notes: **Speaking frame hint:** linking to what we know and correct place value. ... groups of ... tenths is ... tenths. (Do I need to regroup?) For example, 6 groups of 3 tens is 18 ... groups of ... ones is ... ones. (Any regroups to add? Do I need to regroup?) tens (linking to known fact $6 \times 3 = 18$). ... groups of ... tens is ... tens. (Any regroups to add? Do I need to regroup?) This can be regrouped to 1 hundred The product of ... and ... is and 8 tens.

Multiplication

Write ar	atement: d calculate mathematical statements for multiplication w, including for two-digit numbers times one-digit num nethods	
3LS30 Step 2: Introducing the long divi	sion method (sharing ones)	
Concrete	Pictorial	Abstract - Written symbolic
		3 $4 \boxed{13}$ $- \frac{12}{1}$ $13 \div 4 = 3 r 1$
Abstract - Speaking frame		Notes:
I am sharing ones int There are ones in ea I have one(s) remain The quotient is with .	Pupils are introduced to the long division method for the first time in this sequence. Short division will not be introduced until pupils have understood all of the stages in this expanded form. In the calculation $96 \div 4$, for example, pupils often struggle to understand that 1 ten will be regrouped after 8 tens have been used in the 4 groups. This is hidden in short division but recorded in long division.	

Year 3		late mathematical statements for multiplication a uding for two-digit numbers times one-digit numb						
3LS30 Step 3: Long division	3LS30 Step 3: Long division of tens and ones with no regrouping (sharing structure)							
Concret	e	Pictorial	Abstract - Written symbolic					
			$4 2$ $2 8 4$ $- 8 4$ $- 8 4$ $- 4$ $- 4$ $- 4$ $- 0$ $84 \div 2 = 42$					
Abstract - Speaking	g frame		Notes:					
First, I am sharing tens into equal groups. There are tens in each group. I have ten(s) remaining.			This stage is to support pupils' understanding of the abstract notation. They learn to record how many tens are in each group, if there are any tens remaining and what the arrow means.					
Then, I am sharing ones into equal groups. There are ones in each group. I have one(s) remaining. The quotient is with remainders.			Speaking frame note: <i>"First, I am sharing 8 tens into 2 equal groups. There are 4 tens in each group. I have zero tens remaining. Then, I am sharing 4 ones into 2 equal groups. There are 2 ones in each group. I have zero ones remaining. The quotient is 42 with no remainders."</i>					



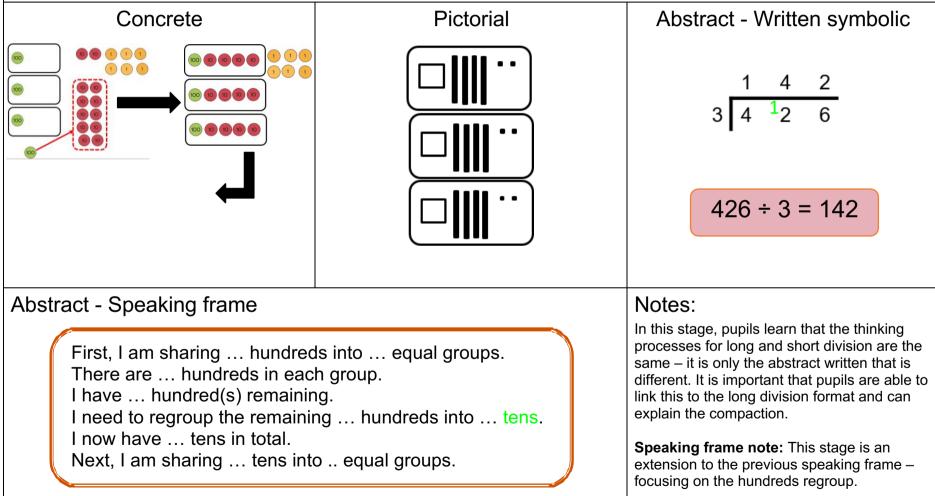




NC Statement:

Pupils practise to become fluent in the formal written method of short multiplication and short division with exact answers (non-statutory guidance)

4LS25 Step 4: Introducing formal short division (sharing structure)



Year 5

Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context

5LS12 Step 2: Introducing formal short division regroup from tens to ones (grouping structure)

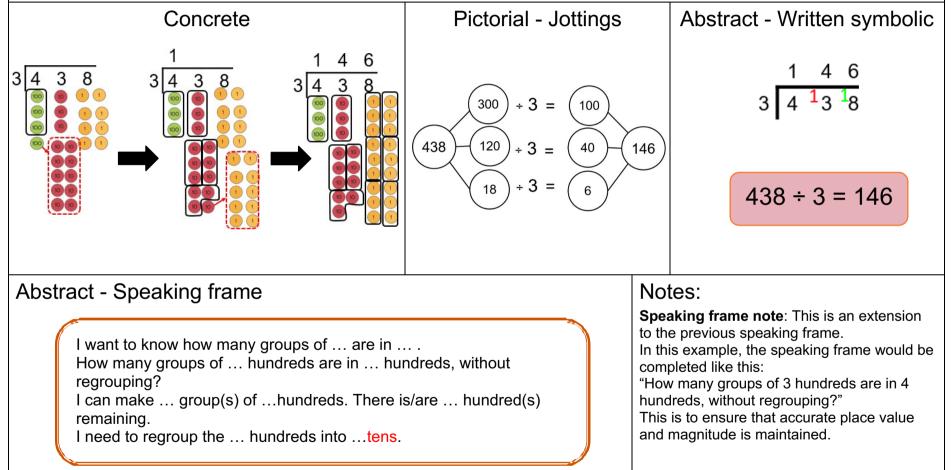
NC Statement:

Concrete **Pictorial - Jottings** Abstract - Written symbolic 4 5 10 4 5 52 13 12 +4 = $52 \div 4 = 13$ Abstract - Speaking frame Notes: Pupils are encouraged to progress to a grouping model of division. This is in I want to know how many groups of ... are in preparation for 2-digit divisors and How many groups of ... tens are in ... tens without regrouping? understanding fractions expressed as part of I can make ... group(s) of ... tens. There is/are ... ten(s) remaining. the quotient. I need to regroup the ... tens into ... ones. Pupils should explore with simple division I now have ... ones. calculations to ensure that they understand How many groups of ... ones are in ... ones, without regrouping? the shift in structure. I can make ... group(s) of ... ones. There is/are ... one(s) remaining. Speaking frame note: In this example, the speaking frame would be completed like this: There are ... groups of ... in ... with ... remainders. "How many groups of 3 tens are in 4 tens, without regrouping?" This is to ensure that accurate place value and magnitude is maintained.

Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context

5LS12 Step 3: Short division for numbers up to 4-digits (grouping structure)

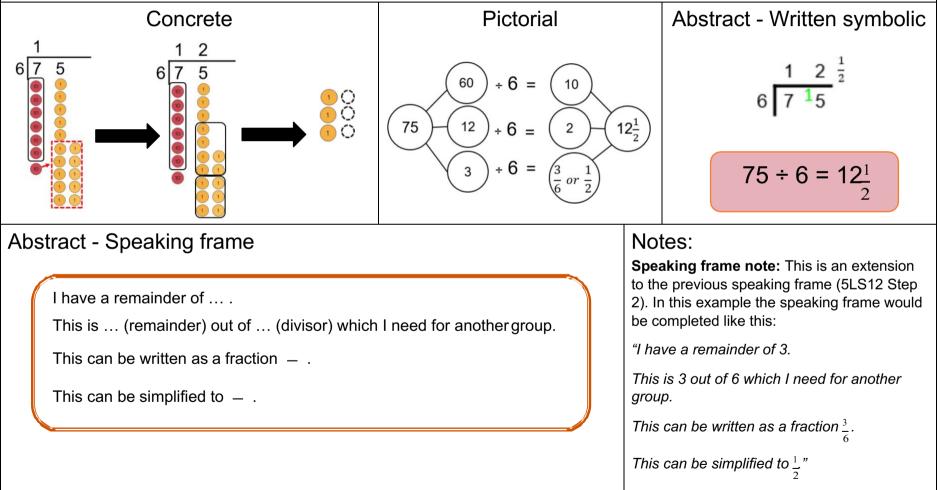
NC Statement:



Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context

5LS12 Step 4: Short division (grouping structure) - expressing quotients with fractions

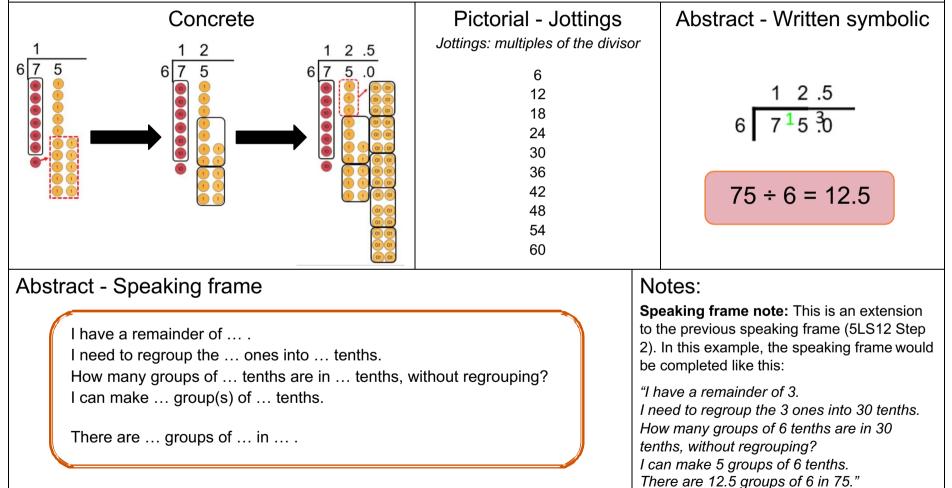
NC Statement:



Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context

5LS12 Step 5: Short division (grouping structure) - expressing quotients with decimals

NC Statement:



NC Statement:

Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division and interpret remainders as whole number remainders , fractions, or by rounding, as appropriate for the context

6LS17 Step 2: Long division for numbers up to 4 digits

Concrete	Pictorial - Jottings	Abstract - Written symbolic
	Jottings: multiples of the divisor 13 26 39 52 65 78 91 104	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
Abstract - Speaking frame	Notes: The structure	of long division was first introduced in
I want to know how many groups of are in How many groups of thousand are inthousand, without regrouping? I can make group(s) ofthousand. There is/are thousan remaining. I need to regroup the thousand(s) intohundreds.	at S30, then re 5. It was revised Jottings are us facts. Speaking fran previous spea example, the st this: "How many gruwithout reground thousand. The	evisited and extended in both years 4 and ed in Step 1 of this sequence. Sed to scaffold to derived related division ne note: This is an extension to the king frame (5LS12 Step 2). In this speaking frame would be completed like oups of 13 thousands are in 3 thousand, ping?" I can make zero groups of 13 re are 3 thousand remaining. I need to thousands into 30 hundreds."

These additional examples show only jottings, completed speaking frames and abstract recording. This complexity of calculation should only be introduced to pupils once they are confident in the conceptual pathway and can explain the abstract recording with reference to the concrete and pictorial models.

Additional Year 6 examples Year 6			using the formal written method of long ders , fractions, or by rounding, as appropriate	
6LS17 Step 4: Long division for n	umbers up to 4 digits - expre	essing quotients with fractions		\triangleright
Abstract speak I have a remained This is 9 out of the 15 we another grow This can be written as This can be simpled There are $37\frac{3}{5}$ in each of	the der of 9. Which I need for up. a fraction $\frac{9}{15}$.	Pictorial - Jottings Jottings: multiples of the divisor 15 30 45 60 75 90 105 120 135 150	Abstract - Written symbolic $ \begin{array}{r} 0 & 3 & 7 & \frac{3}{5} \\ 15 & 5 & 6 & 4 \\ - & 0 & 4 & 5 & 4 \\ - & 0 & 4 & 5 & 4 \\ - & 4 & 5 & 4 & 4 \\ - & 1 & 0 & 5 & 9 \\ \frac{9}{15} = \frac{3}{5} \\ \end{array} $ $ \begin{array}{r} 9 \\ 9 \\ 15 \\ 564 \div 15 = 37 \frac{3}{5} \end{array} $	Additional Year 6 examples

Additional Year 6 examples	NC Statement:			
Year 6	Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division and interpret remainders as whole number remainders , fractions, or by rounding, as appropriate for the context			
61 S17 Step 5: Long division for numbers up to 4 digits - expressing quotients with decimals				

6LS17 Step 5: Long division for numbers up to 4 digits - expressing quotients with decimals

Abstract speaking frame	Pictorial - Jottings Jottings: multiples of the divisor	Abstract - Written symbolic
I have a remainder of 9. I need to regroup the 9 ones into 90 tenths. How many groups of 15 tenths are in 90 tenths, without regrouping? I can make 6 groups of 15 tenths. There is nothing remaining. There are 37.6 groups of 15 in 564.	15 30 45 60 75 90 105 120 135 150	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$

Additional Year 6 examples

Additional Year 6 examples Year 6	NC Statement: Multiply multi-digit numbers of up of long multiplication	o to 4-digits by a two-digit whole	e number using the formal written method	
6LS12 Step 3: Long multiplication; Abstract spe		Pictorial - Jottings Jottings: multiples of tricky	Abstract - Written symbolic	Ado
First, I need to consider th 7 groups of 6 on I need to regroup into 7 groups of 3 te I need to add the regrouped I need to add the regrouped hundreds. I can regroup the hundreds. I can regroup the hundreds. I can regroup the 20 groups of 6 on I need to regroup into 1 20 groups of 3 ten I need to add the regrouped hundred 20 groups of 8 hundred is 1 regroups The total of the two partie The product of 836 a	 a 4 tens and 2 ones. b 4 tens and 2 ones. c hundreds and 5 tens. c hundreds and 5 tens. c hundreds and 5 tens. c hundreds. c hundreds. I now have 58 d is into 5 thousands and 8 eds. c tens in the multiplier. a is 6 hundreds. d 1 hundred. I now have 7 eds. d thousand. There are no to add. a products is 22, 572. 	multipliers 7 14 21 28 35 42 49 56 63 70 77 84	$2 \frac{1}{4}$ 8 3 6 x 2 7 5 8 5 2 167 2 0 225 7 2 1 1 836 x 27 = 22,572	Additional Year 6 examples